Quantum model for Impulsive Stimulated Raman Scattering (ISRS)

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Outline



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Introduction

The model Experiment 1: mode occupation numbers Experiment 2: quadrature Conclusion

INCEPT

INhomogenieties and fluctuations in quantum CohErent Phases by ultrafast optical Tomography

- Experiments: Prof. Daniele Fausti (P.I.), Theory: Prof. Fabio Benatti
- Ultrashort dynamics in complex materials (sub-picosecond time scales)
- Cross-fertilization between quantum optics (quantum state tomography) and condensed matter physics (pump-probe experiments)

Introduction

The model Experiment 1: mode occupation numbers Experiment 2: quadrature Conclusion

Pump-probe experiments



- Pump pulse excites the material
- Probe pulse (less intense) test the evolution after a delay time t

Introduction

The model Experiment 1: mode occupation numbers Experiment 2: quadrature Conclusion

Raman scattering

- Raman scattering is a kind of inelastic scattering for light
- One photon loses energy exciting one phonon in the material (Stokes process)... or
 One photon increases its energy destroying one phonon (anti-Stokes process)



Probe-target interaction

- Initial state (probe + target): $|\alpha\rangle\langle\alpha|\otimes\varrho_t$
- Refraction at the boundary

$$\mathcal{H}_{\mathsf{ref}} = \sum_{j,\mu,\mu'} \left(\eta^{(0)}_{\mu\mu'} + \langle \boldsymbol{b} + \boldsymbol{b}^{\dagger}
angle_t \eta^{(1)}_{\mu\mu'}
ight) \left(\boldsymbol{a}^{\dagger}_{\mu j} \, \boldsymbol{r}_{\mu' j} + \, \boldsymbol{a}_{\mu j} \, \boldsymbol{r}^{\dagger}_{\mu' j}
ight)$$

Raman scattering

$$H_{Ram} := \sum_{\mu,\mu'} \chi_{\mu,\mu'} \left[\left(\sum_{j} a^{\dagger}_{\mu j} a_{\mu' j + \frac{\Omega}{\delta}} \right) b^{\dagger} + \left(\sum_{j} a_{\mu j} a^{\dagger}_{\mu' j + \frac{\Omega}{\delta}} \right) b \right],$$

 $a_{\mu j}, r_{\mu j}, b$ are bosonic operators

Dynamics and observables

Evolution operator

$$U(au) = U_{bulk}(au) U_{ref}$$

$$U_{ref} = \exp(-i H_{ref}) , \quad U_{bulk}(\tau) = \exp(-i \tau H_{Raman}) \qquad (\hbar = 1) ,$$

Average of an observable X_{phot}

$$\langle X_{phot}(\tau) \rangle_t = \operatorname{Tr}[U(\tau) | \alpha \rangle \langle \alpha | \otimes \varrho_t \ U^{\dagger}(\tau) \ X_{phot}]$$

Coherent state of the probe

$$\begin{split} |\alpha\rangle &= \exp\Big(\sum_{j} \alpha_{xj} a_{xj}^{\dagger} - \alpha_{xj}^{*} a_{xj}\Big) |0\rangle \ , \quad a_{xj} |\alpha\rangle = \alpha_{xj} \ , \quad a_{yj} |\alpha\rangle = 0 \ , \\ \alpha_{xj} &= \exp\left(-\frac{(j\delta)^{2}}{2\sigma^{2}}\right) e^{i\varphi} \end{split}$$

Pump-target interaction

- Same Hamiltonian for the light-matter interaction but different approximation
- Mean field for photons $a_{\lambda j} \rightarrow \alpha^{P}_{\lambda j}$
- Explicit dependence on the polarization angle (with respect to x)

$$\alpha_{xj}^{P} = \alpha_{0j}^{P} \cos(\theta_{P}), \quad \alpha_{yj}^{P} = \alpha_{0j}^{P} \sin(\theta_{P})$$

• Phononic operator shifted $\langle b \rangle_t = \text{Tr}(\varrho_t b) = \text{Tr}(\varrho b_t)$

$$egin{aligned} b o b_t = & U_{ ext{ref}}^\dagger \; U_{ ext{bulk}}^\dagger(au) \, U_{ ext{free}}^\dagger(t) \, b \, U_{ ext{free}}(t) \, U_{ ext{bulk}}(au) \, U_{ ext{ref}} \ & \simeq & \mathrm{e}^{-i\Omega t} \left(b - i au \sum_{j,\lambda\lambda'} \chi_{\lambda\lambda'} \, lpha_{\lambda j}^{P*} \, lpha_{\lambda' j + rac{\Omega}{\delta}}^P
ight). \end{aligned}$$

Assumptions on the interaction (good for Quartz)

Zeroth order refraction matrix

$$\eta^{(0)} = egin{pmatrix} \eta^{(0)}_{xx} & \eta^{(0)}_{xy} \ \eta^{(0)}_{xy} & \eta^{(0)}_{xx} \end{pmatrix}$$

 First order refraction matrix depending on the phonon involved (same for *χ*)

$$\begin{aligned} \mathbf{A} : \eta^{(1)} &= \begin{pmatrix} \eta_{xx}^{(1)} & \mathbf{0} \\ \mathbf{0} & \eta_{xx}^{(1)} \end{pmatrix}, \quad \mathbf{E}_{L} : \eta^{(1)} &= \begin{pmatrix} \eta_{xx}^{(1)} & \mathbf{0} \\ \mathbf{0} & -\eta_{xx}^{(1)} \end{pmatrix}, \\ \mathbf{E}_{T} : \eta^{(1)} &= \begin{pmatrix} \mathbf{0} & \eta_{xy}^{(1)} \\ \eta_{xy}^{(1)} & \mathbf{0} \end{pmatrix} \end{aligned}$$

Geometry

 Phonons selected by the angle between the polarization of the pump and the x axis (θ_P)

$$\begin{aligned} \mathbf{A} : \langle \mathbf{b} \rangle_t &= C_A \mathrm{e}^{-i\Omega_A t - i\pi/2} \\ \mathbf{E}_L : \langle \mathbf{b} \rangle_t &= C_E \cos(2\theta_P) \, \mathrm{e}^{-i\Omega_E t - i\pi/2} , \\ \mathbf{E}_T : \langle \mathbf{b} \rangle_t &= C_E \sin(2\theta_P) \, \mathrm{e}^{-i\Omega_E t - i\pi/2} , \end{aligned}$$

Remember:

$$egin{aligned} & p
ightarrow U_{\textit{ref}}^{\dagger} \; U_{\textit{bulk}}^{\dagger}(au) \; U_{\textit{free}}^{\dagger}(t) \; b \; U_{\textit{free}}(t) \; U_{\textit{bulk}}(au) \; U_{\textit{ref}} \ & \simeq \mathrm{e}^{-i\Omega t} \left(b - i au \sum_{j,\lambda\lambda'} \chi_{\lambda\lambda'} \; lpha_{\lambda j}^{\mathcal{P}*} \; lpha_{\lambda' j + rac{\Omega}{\delta}}^{\mathcal{P}}
ight). \end{aligned}$$

Mode occupation numbers (y polarization)

$$\begin{split} \langle \mathcal{N}_{yk}(\tau) \rangle_t \simeq & \langle \mathbf{b} + \mathbf{b}^{\dagger} \rangle_t |\alpha_{xk}|^2 \, \mathcal{F}_{ref}^y \\ & -i \, \langle \mathbf{b}^{\dagger} - \mathbf{b} \rangle_t |\alpha_{xk}| \left(|\alpha_{xk+\frac{\Omega}{\delta}}| - |\alpha_{xk-\frac{\Omega}{\delta}}| \right) \, \mathcal{F}_{Ram}^y(\tau) \end{split}$$

$$\begin{array}{ll} A: & F_{ref}^{y} = 0, & F_{Ram}^{y}(\tau) = 0, \\ E_{L}: & F_{ref}^{y} = 0, & F_{Ram}^{y}(\tau) = 0, \\ E_{T}: & F_{ref}^{y} = 2\eta_{xy}^{(1)}\eta_{xy}^{(0)}\sin^{2}(\eta_{xx}^{(0)}), & F_{Ram}^{y}(\tau) = 0. \end{array}$$



- Pump at 45°: A and E_T phonons excited
- Orthogonal polarization (leading term): E_T Refractive

Mode occupation numbers (x polarization)

$$\begin{split} \langle N_{xk}(\tau) \rangle_t \simeq &\cos^2(\eta_{xx}^{(0)}) |\alpha_{xk}|^2 + \langle b + b^{\dagger} \rangle_t |\alpha_{xk}|^2 \, F_{ref}^x \\ &- i \, \langle b^{\dagger} - b \rangle_t |\alpha_{xk}| \left(|\alpha_{xk + \frac{\Omega}{\delta}}| - |\alpha_{xk - \frac{\Omega}{\delta}}| \right) \, F_{Ram}^x(\tau) \end{split}$$

$$\begin{aligned} \mathbf{A} : \quad F_{ref}^{x} &= -\eta_{xx}^{(1)} \sin(2\eta_{xx}^{(0)}), \qquad F_{Ram}^{x}(\tau) &= \chi_{xx}\tau \cos^{2}(\eta_{xx}^{(0)}), \\ E_{L} : \quad F_{ref}^{x} &= -\eta_{xx}^{(1)} \sin(2\eta_{xx}^{(0)}), \qquad F_{Ram}^{x}(\tau) &= \chi_{xx}\tau \cos^{2}(\eta_{xx}^{(0)}), \\ E_{T} : \quad F_{ref}^{x} &= -2\eta_{xy}^{(1)}\eta_{xy}^{(0)} \cos^{2}(\eta_{xx}^{(0)}), \qquad F_{Ram}^{x}(\tau) &= 0. \end{aligned}$$



- Pump at 0°: A and E_L phonons excited
- Parallel polarization: Raman and Refractive effects are both visible

Results Experiment 1 (summary)

- Phase mismatch between Raman and refractive modulation
- Selection of different phonons according to the polarization of the pump
- Different behaviour of Raman and refractive modulation depending on the phonon involved and on the polarization selected by the analyzer
- Good agreement between theory and experiment

Quadrature: Homodyne detection + Time-resolved spectroscopy



 We combine two different experimental techniques to probe the nonequilibrium response of the material

Average quadrature

Measured quantity: Current difference I

$$I = \sum_{j} \left(c_{xj}^{\dagger} c_{xj} - d_{xj}^{\dagger} d_{xj} \right), \qquad c_{j} = \frac{a_{xj} + a_{xj}^{LO}}{\sqrt{2}}, \ d_{j} = \frac{a_{xj} - a_{xj}^{LO}}{\sqrt{2}}$$

Quadrature:

$$X_{s} = rac{1}{\sqrt{2}} \, \sum_{j} \left(a_{xj} \, z_{j}^{*} \, \mathrm{e}^{-i \Phi_{j}(s)} \, + \, a_{xj}^{\dagger} \, z_{j} \, \mathrm{e}^{i \Phi_{j}(s)}
ight) \propto I$$

• Theoretical prediction:

•

$$\langle X_{s}(\tau) \rangle = \mathcal{A}_{t} \cos(\omega_{0} s + \Phi_{t})$$

where

$$\mathcal{A}_t \simeq \mathcal{A}\left(1 + \overline{\eta}\sin(\Omega t)\right), \quad \Phi_t \simeq 2\overline{\chi}\sin(\Omega t).$$

Average quadrature

$$\mathcal{A}_t \simeq \mathcal{A}\left(1 + \overline{\eta}\sin(\Omega t)\right), \quad \Phi_t \simeq 2\overline{\chi}\sin(\Omega t).$$



Variance of the quadrature: work in progress



- For a coherent initial state: variance is time-independent up to second order in the coupling
- Higher order effects or (more likely) signature of a statistical mixture

Conclusions and Outlook

Results:

- Fully quantum model for Impulsive Stimulated Raman Scattering (ISRS)
- Outcomes of two different experiments correctly reproduced

Future work:

- Complete tomography of the state of light (variance of the quadrature)
- Role of quantum correlations
- More interesting (complex) dynamics in the sample (*e.g.* interaction between the vibrational and electronic degrees of freedom)

Thank you for your attention!

Social dinner: Pizzeria "Al Barattolo" at 20.00.